

Solving Linear Equations and Inequalities Review

Key

Solve each equation.

$$1. \quad 2(7 + 5y) - 3y = -35$$

$$14 + 10y - 3y = -35$$

$$14 + 7y = -35$$

$$7y = -49$$

$$y = -7$$

$$2. \quad 7x + 5 = 12x - 10$$

$$7x + 10 = -7x + 10$$

$$15 = 5x$$

$$3 = x$$

$$3. \quad -1 = \frac{5+x}{6}$$

$$-6 = 5 + x$$

$$-11 = x$$

Solve each inequality. Describe the solution set using interval notation. Then graph the solution set on a number line.

$$4. \quad 4x - 6 < 18$$

$$+6 \quad +6$$

$$\frac{4x}{4} < \frac{24}{4}$$

$$x < 6$$

$$5. \quad -x < -x + 7(x - 2)$$

$$-x < -x + 7x - 14$$

$$-x < 6x - 14$$

$$-6x \quad -6x$$

$$-7x < -14$$

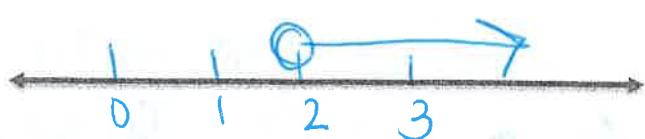
$$x > 2$$

Interval Notation

$$(-\infty, 6)$$

Interval Notation

$$(2, \infty)$$



Solve each absolute value equation.

$$6. \quad 4|n + 8| = 56$$

$$|n + 8| = 14$$

$$n + 8 = 14$$

$$n = 6$$

$$n + 8 = -14$$

$$n = -22$$

$$7. \quad 2|x + 4| + 3 = 9$$

$$2|x + 4| = 6$$

$$|x + 4| = 3$$

$$x + 4 = 3$$

$$x = -1$$

$$x + 4 = -3$$

$$x = -7$$

Solve each inequality. Describe the solution set using interval notation. Then, graph the solution set on a number line.

$$8. -10b + 3 \leq -37 \text{ or } 3b - 10 \leq -25$$

$$\begin{array}{rcl} -3 & -3 & +10 & +10 \\ -10b \leq -40 & & 3b \leq -15 & \\ b \geq 4 & \text{or} & b \leq -5 & \end{array}$$

$$9. -50 < 7k + 6 < -8$$

$$\begin{array}{rcl} -6 & -6 & -6 \\ -56 < 7k < -14 & & \\ -8 < k < -2 & & \\ k > -8 \text{ and } k < -2 & & \end{array}$$

Interval Notation $(-\infty, -5] \cup [4, \infty)$ Interval Notation $(-\infty, -2)$



Solve each absolute value inequality. Describe the solution set using interval notation. Then, graph the solution set on a number line.

$$10. |7x + 4| \geq 74$$

$$\begin{array}{l} 7x + 4 \geq 74 \text{ or } 7x + 4 \leq -74 \\ 7x \geq 70 \quad 7x \leq -78 \\ x \geq 10 \quad \text{or} \quad x \leq -11.1 \end{array}$$

$$11. |x + 5| < 9$$

$$\begin{array}{l} x + 5 < 9 \quad x + 5 > -9 \\ x < 4 \quad \text{and} \quad x > -14 \end{array}$$

Interval Notation $(-\infty, -11.1] \cup [10, \infty)$

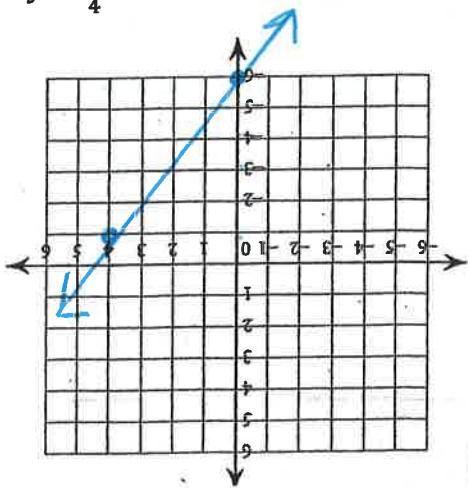


Interval Notation $(-14, 4)$

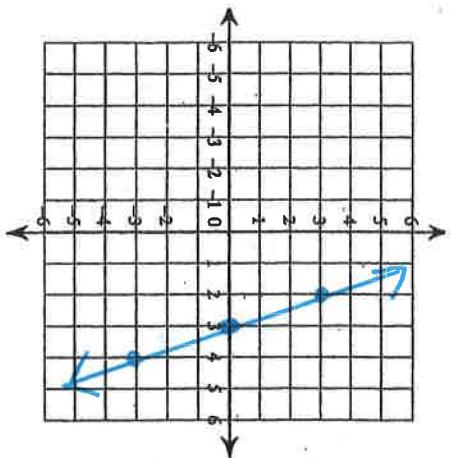


Sketch the graph of each line.

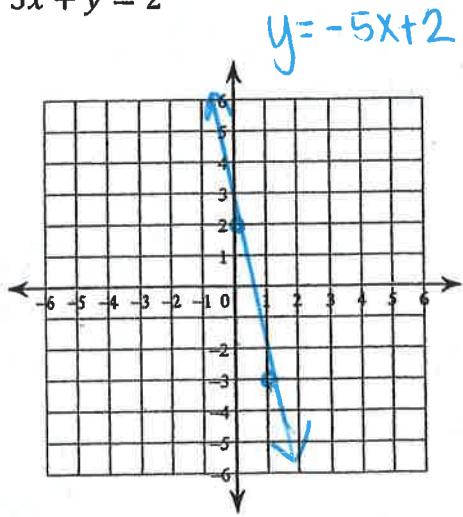
12. $y = \frac{5}{4}x + 6$



13. $y = \frac{1}{3}x - 3$

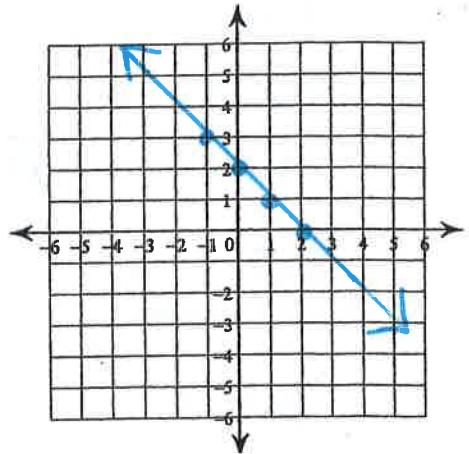


14. $5x + y = 2$

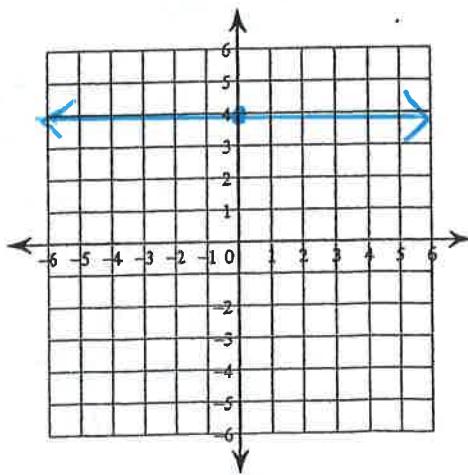


15. $x + y = 2$

$y = -x + 2$

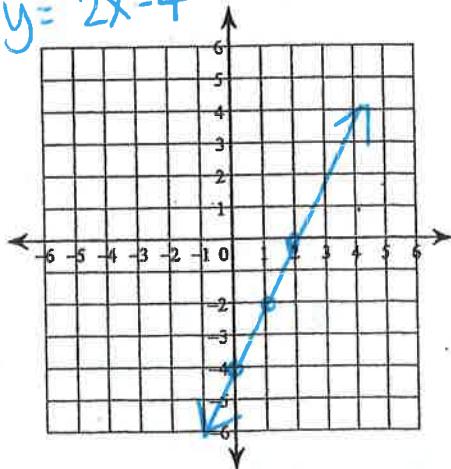


16. $y = 4$



17. $2x - y = 4$

$-y = -2x + 4$
 $y = 2x - 4$



Write an equation in slope-intercept form that passes through the given point and has the given slope.

18. $m = \frac{1}{4}$ through $(-4, 2)$

$$2 = \frac{1}{4}(-4) + b$$

$$2 = -1 + b$$

$$3 = b$$

$$y = \frac{1}{4}x + 3$$

19. $m = -3$ through $(2, -5)$

$$-5 = -3(2) + b$$

$$-5 = -6 + b$$

$$1 = b$$

$$y = -3x + 1$$

Write the slope-intercept form of the line that passes through each pair of points.

20. $(2, 3)$ and $(4, -2)$

$$\frac{3 - (-2)}{2 - 4} = \frac{5}{-2}$$

$$3 = -\frac{5}{2}(2) + b$$

$$3 = -5 + b$$

$$b = 8$$

$$y = -\frac{5}{2}x + 8$$

$$\frac{10 - 13}{10 - 14} = \frac{-3}{-6} = \frac{1}{2}$$

$$10 = \frac{1}{2}(8) + b$$

$$10 = 4 + b$$

$$6 = b$$

$$y = \frac{1}{2}x + 6$$

Write the slope-intercept form of an equation that passes through the points and is parallel to the graph of each equation.

22. through $(-1, 3)$, $y = -3x + 4$

$$m = -3$$

$$3 = -3(-1) + b$$

$$3 = 3 + b$$

$$0 = b$$

$$y = -3x$$

23. through $(4, 8)$, $6x + y = 2$

$$y = -6x + 2$$

$$m = -6$$

$$8 = -6(4) + b$$

$$8 = -24 + b$$

$$32 = b$$

$$y = -6x + 32$$

Write the slope-intercept form of an equation that passes through the point and is perpendicular to the graph of each equation.

24. $(2, 5)$, $3x + 5y = 7$

$$5y = -3x + 7$$

$$y = -\frac{3}{5}x + \frac{7}{5}$$

$$m = -\frac{3}{5}$$

$$5 = \frac{5}{3}(2) + b$$

$$5 = \frac{10}{3} + b$$

$$\frac{5}{3} = b$$

$$y = \frac{5}{3}x + \frac{5}{3}$$

25. $(0, -4)$, $6x - 3y = 5$

$$-3y = -6x + 5$$

$$y = 2x - \frac{5}{3}$$

$$m = -\frac{1}{2}$$

$$y = -\frac{1}{2}x - 4$$