

Geometry Notes

Introduction: Congruent Triangles

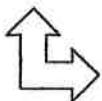
Name: NOTES

Recall: There are 3 transformations that preserve size and shape – just simply change original location:

1. Reflection

2. Translation

3. Rotation



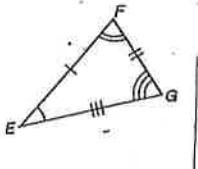
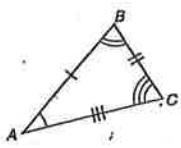
All 3 types are examples of Rigid transformations!

*Properties of Congruent Triangles:

1. Corresponding Angle are Congruent

2. Corresponding Sides are Congruent

SO: If $\triangle ABC \cong \triangle EFG$, the vertices of the two triangles correspond in the same order as the letters naming the triangles.



$$\angle A \cong \angle E$$

$$\angle B \cong \angle F$$

$$\angle C \cong \angle G$$

$$\overline{AB} \cong \overline{EF}$$

$$\overline{BC} \cong \overline{FG}$$

$$\overline{AC} \cong \overline{EG}$$

Ex1: Name the congruent angles and sides for each pair of congruent triangles.

A) $\triangle TUV \cong \triangle XYZ$

$$\begin{array}{ll} \angle T \cong \angle X & \overline{TU} \cong \overline{XY} \\ \angle U \cong \angle Y & \overline{UV} \cong \overline{YZ} \\ \angle V \cong \angle Z & \overline{TV} \cong \overline{XZ} \end{array}$$

B) $\triangle CDG \cong \triangle RSW$

$$\begin{array}{ll} \angle C \cong \angle R & \overline{CD} \cong \overline{RS} \\ \angle D \cong \angle S & \overline{DG} \cong \overline{SW} \\ \angle G \cong \angle W & \overline{CG} \cong \overline{RW} \end{array}$$

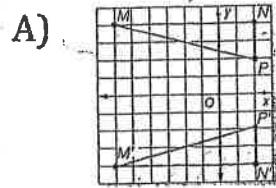
C) $\triangle ABCF \cong \triangle DGH$

$$\begin{array}{ll} \angle B \cong \angle D & \overline{BC} \cong \overline{DG} \\ \angle C \cong \angle G & \overline{CF} \cong \overline{GH} \\ \angle F \cong \angle H & \overline{BF} \cong \overline{DH} \end{array}$$

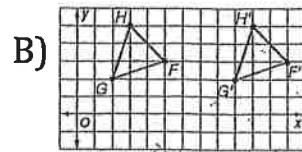
D) $\triangle ADG \cong \triangle HKL$

$$\begin{array}{ll} \angle A \cong \angle H & \overline{AD} \cong \overline{HK} \\ \angle D \cong \angle K & \overline{DG} \cong \overline{KL} \\ \angle G \cong \angle L & \overline{AG} \cong \overline{HL} \end{array}$$

Ex2: Identify the congruent triangles in each figure. Then, name the congruence transformation.



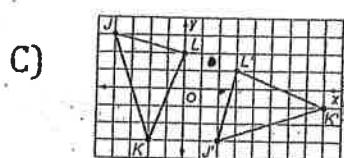
Reflection over
x-axis $(x, -y)$
 $\Delta MNP \cong \Delta M'N'P'$



~~Rotation~~

translation
 $(x+3, y)$

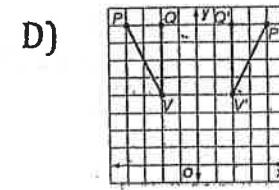
$\Delta FGH \cong \Delta F'G'H'$



$(-4, 1) \rightarrow (2, 1)$
 $(0, 1) \rightarrow (3, 1)$
 $(2, -1) \rightarrow (8, -1)$

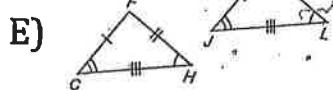
Rotate ~~180°~~

$\Delta JKL \cong \Delta J'K'L'$



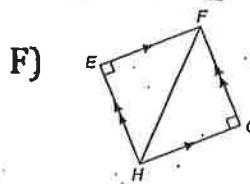
$\Delta V'PQ \cong \Delta V'Q'P'$

Reflect over
y-axis



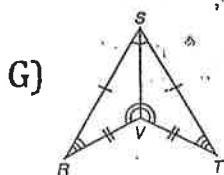
Translation

$\Delta CDFH \cong \Delta JKLF$



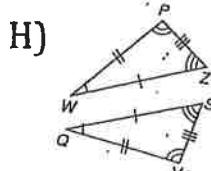
Reflect over \overline{HF} ~~180°~~

$\Delta HEF \cong \Delta HGF$



Reflect over SV

$\Delta SRV \cong \Delta STV$



Reflection

$\Delta PZW \cong \Delta VSQ$



Do $\Delta ABC \cong \Delta DEF$

