

1. Which expression is equivalent to

$$\frac{2x+6}{x^2+2x-24} \cdot \frac{x^2+2x-24}{x^2-7x+12}?$$

A $\frac{2}{x-4}$ $\frac{2(x+3)}{(x-4)(x+6)} \cdot \frac{(x-4)(x+6)}{(x-4)(x-3)}$

B $\frac{2(x+3)}{x-3}$ $\frac{2(x+3)}{(x-4)(x-3)}$

C $\frac{2(x+3)}{(x-4)(x-3)}$

D $\frac{2(x+3)}{(x+4)(x-3)}$

2. Which expression is equivalent to

$$\frac{x+3}{6x-3} \div \frac{x^2+2x-3}{2x-1}$$

A $3(x-1)$

B $\frac{x-1}{3}$

C $\frac{3}{x-1}$

D $\frac{1}{3(x-1)}$

$$\frac{x+3}{6x-3} \times \frac{2x-1}{x^2+2x-3}$$

$$\frac{x+3}{3(2x-1)} \times \frac{2x-1}{(x-1)(x+3)} = \frac{1}{3(x-1)}$$

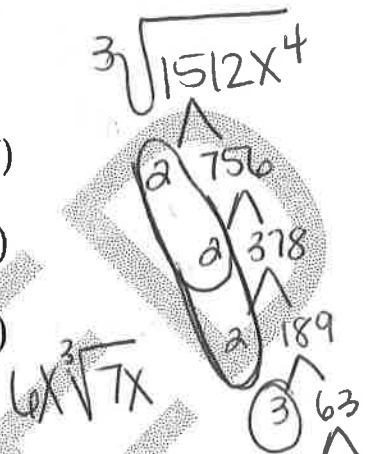
3. Multiply: $\sqrt[3]{12x^2} \cdot \sqrt[3]{126x^2}$

A $6x(\sqrt[3]{7x})$

B $6x(\sqrt[3]{21x})$

C $6x^2(\sqrt[3]{42})$

D $6x^2(\sqrt[3]{63})$



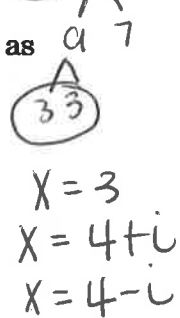
4. Which polynomial function has as zeros 3 and 4 + i?

A $f(x) = x^3 - 11x^2 + 41x - 51$

B $f(x) = x^3 - 5x^2 - 7x + 51$

C $f(x) = x^3 + 5x^2 - 7x - 51$

D $f(x) = x^3 + 11x^2 + 41x + 51$



$(x-3)(x-4+i)(x-4-i)$
 $x^2 - 4x - ix - 4x + ix + 16 - 4i + 4i - i^2$
 $(x-3)(x^2 - 8x + 17) = x^3 - 3x^2 - 8x^2 + 24x + 17x - 51$

5. If $h(x) = 2x$ and $g(x) = 3x^2 + 1$, what is $h(g(x))$?

A $6x^2 + 1$

B $6x^2 + 2$

C $12x^2 + 1$

D $12x^2 + 2$

$2(3x^2 + 1)$
 $6x^2 + 2$

22. Let x and y be real numbers. If $(x + yi) - (2 - 3i) = -6 + 4i$, what are the values of x and y ?

- A $x = 8, y = 7$
 - B $x = 8, y = 1$
 - C $x = -4, y = 7$
 - D $x = -4, y = 1$
- Handwritten work:
 $x - 2 = -6$
 $x = -4$
 $yi - -3i = 4i$
 $yi = 1i$
 $y = 1$

23. If $f(x) = 2x + 1$ and $g(x) = x^3$, what is $f(g(3))$?

- A 343
- B 189
- C 55
- D 34

Handwritten work:
 $g(3) = 3^3 = 27$
 $f(27) = 2(27) + 1$
 $= 55$

24. In which direction does the graph of $y = (x + 2)^{\frac{1}{2}} + c$ shift as c decreases?

- A right
 - B left
 - C up
 - D down
- Handwritten notes:
 c moves graph along y axis
 \uparrow or \downarrow
 If $c \downarrow$ so does the graph

25. What is the value of z in the solution of this system?

- A -7
 - B -1
 - C 3
 - D 5
- Handwritten work:
 $x + y - z = -5$
 $2x + z + 1 = -2y$
 $x - y = 3z + 3$
 make sure all variables line up!
 $x + y - z = -5$
 $2x + 2y + z = -1$
 $x - y - 3z = 3$

put into matrix (3x4)
 3 rows, 4 columns

$$\begin{bmatrix} 1 & 1 & -1 & -5 \\ 2 & 2 & 1 & -1 \\ 1 & -1 & -3 & 3 \end{bmatrix}$$

calculate rref

$$\begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & 1 & 0 & -7 \\ 0 & 0 & 1 & 3 \end{bmatrix}$$

Handwritten solution:
 $x = 5$
 $y = -7$
 $z = 3$

26. What is the domain of $f(x) = -2x^3 + x^2 + 1$?

- A the set of all real numbers
- B $\{x | -3 < x < 2\}$
- C $\{x | -2 < x < 3\}$
- D the empty set

Graph it!
Any values x can't be?

27. The population of a small town in North Carolina is 4,000, and it has a growth rate of 3% per year. Which expression can be used to calculate the town's population x years from now?

- A $3(4,000)^x$
- B $4,000(1.03)^x$
- C $4,000x^{1.03}$
- D $4,000x^3$

$y = a b^x$
a = start value
b = increase
x = # of years

28. The graph of $f(x) = x^2 + 3$ is translated to produce the graph of $g(x) = (x + 2)^2 + 3$. In which direction was the graph of f translated?

- A up
- B down
- C left
- D right

Graph them both
look at how it moved

29. Solve for x : $\frac{x-1}{x+5} = \frac{x}{2(x+5)}$

- A -5
- B 2
- C -5 or 2
- D 5 or -2

$\frac{x-1}{x+5} \rightarrow \frac{x}{2x+10}$

$x(x+5) = (2x+10)(x-1)$
 $x^2 + 5x = 2x^2 - 2x + 10x - 10$

-5 makes denominator = 0.

$x^2 + 5x = 2x^2 + 8x - 10$
 $x^2 + 3x - 10 = 0$
 $(x-2)(x+5)$
 $\boxed{x=2} \quad \boxed{x=-5}$

31. Which graph represents the system of inequalities below?

$$2x - 3y \geq 9$$

$$4x + 2y < 8$$

$$2y < -4x + 8$$

$$y < -2x + 4$$

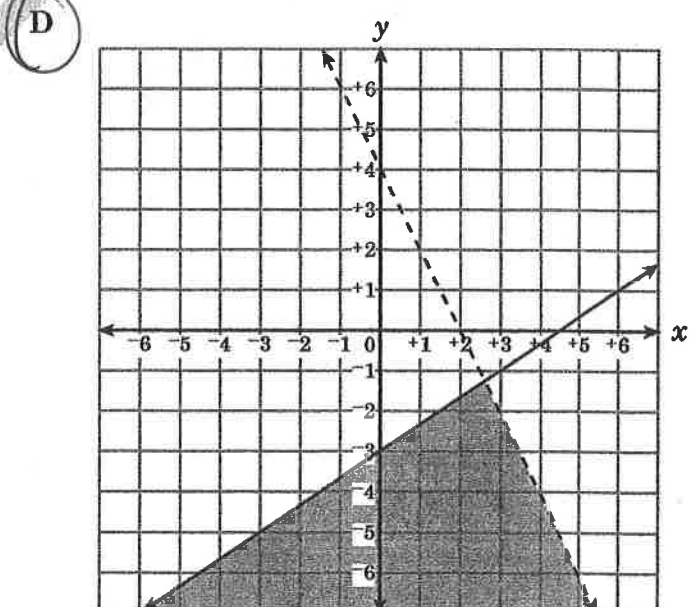
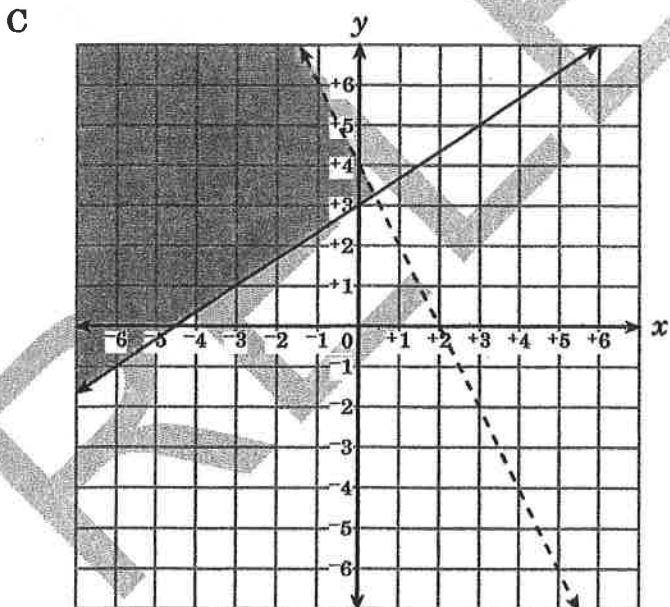
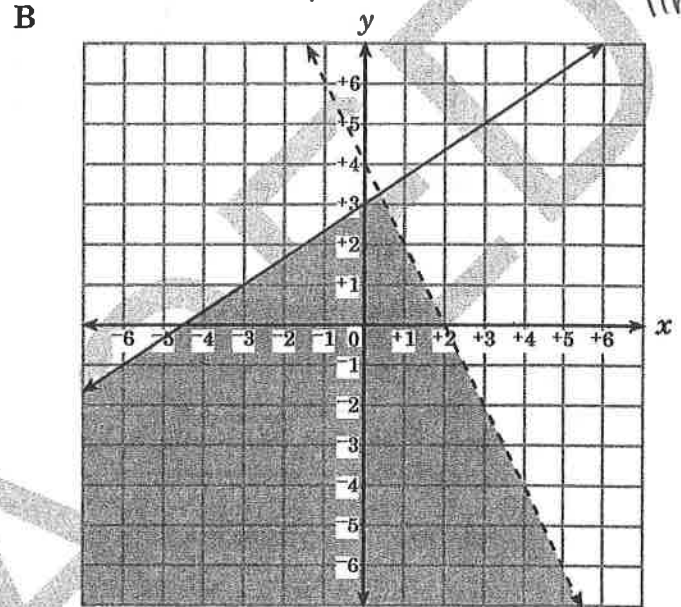
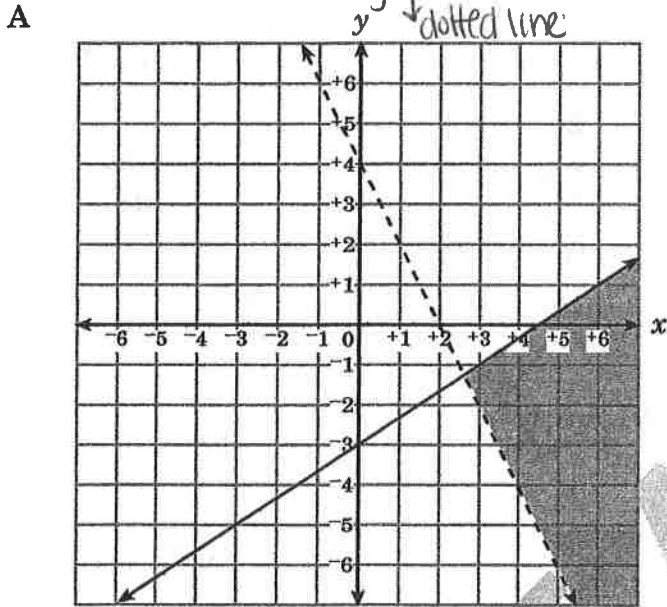
y ↓ dotted line

$$-3y \geq -2x + 9$$

$$y \leq \frac{2}{3}x - 3$$

↑ solid line

both less
So shade
below
each
line



35. Simplify:

$(x^{\frac{3}{4}})^3$ power to power - multiply exponents

- A $x^{\frac{27}{64}}$
- B $x^{\frac{9}{4}}$
- C $x^{\frac{9}{12}}$
- D $x^{\frac{15}{4}}$

36. The area of a rectangular window is $(4x^2 - 21x - 18)$. Both the length and the width are polynomials with integer coefficients. Which of the following could represent the length of the window?

- A $4x + 6$
- B $4x + 3$
- C $x + 6$
- D $x + 3$

$A = l \cdot w$
 $A = 4x^2 - 21x - 18$
 ↑
 factor
 use rainbow method
 $x^2 - 21x - 72$
 $(x + \frac{3}{4})(x - 24)$
 $(4x + 3)(x - 4)$

37. Which binomial is a factor of $((x^3 - x^2) + (3x - 3))$?

- A $x - 3$
- B $x + 1$
- C $x^2 - 1$
- D $x^2 + 3$

Factor by grouping or use synthetic division

OR Graph - zero at 1

$$\begin{array}{r|rrrr} 1 & 1 & -1 & 3 & -3 \\ & & \downarrow & & \\ & & 1 & 0 & 3 \\ \hline & & 1 & 0 & 3 & 0 \end{array}$$

38. If 5 tractors can plow a field in 4 hours, how many hours will it take 3 tractors to plow the field?

- A $6\frac{2}{3}$
- B $6\frac{1}{2}$
- C $5\frac{2}{3}$
- D $5\frac{1}{2}$

$(x^2 + 3)$
 $(x - 1)$

$5 \times \frac{4}{3}$

Inverse variation

39. Solve: $3x - 7\sqrt{x} + 2 = 0$

A $x = \frac{1}{9}, x = 4$

B $x = \frac{1}{3}, x = 4$

C $x = \frac{1}{9}, x = -\frac{1}{3}$

D $x = \frac{1}{3}, x = \frac{1}{9}$

plug in values to check

40. What is the **approximate** value of the greatest zero of $f(x) = x^3 - 6x^2 - x + 3$?

A -0.75

B 2.84

C 6.08

D 6.31

graph - find furthest x-intercept

41. What are the vertical asymptotes of

the function $f(x) = \frac{4x^2 - 100}{2x^2 + x - 15}$?

A $x = -5, x = 5$

B $x = -5, x = 4, x = 5$

C $x = -3, x = \frac{5}{2}$

D $x = -3, x = \frac{5}{2}, x = \frac{20}{3}$

factor denominator

$2x^2 + x - 15$

$x^2 + x - 30$

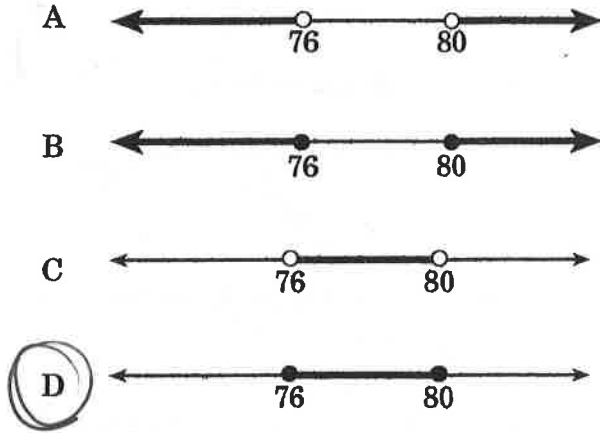
$(x-5)(x+6)$

$(x - \frac{5}{2})(x+3)$

$(2x-5)(x+3)$

$x = \frac{5}{2} \quad x = -3$

42. A poll shows that it is likely that, with a margin of error of ± 2 percentage points, 78% of those randomly selected from a population would vote for a particular candidate. This situation can be described by the inequality $|x - 78| \leq 2$. Which graph shows the percentage of voters (according to the inequality) who favor the candidate?



$x - 78 \leq 2$ $x - 78 \geq -2$
 $x \leq 80$ $x \geq 76$
 $76 \leq x \leq 80$

43. Which equation represents the graph of $y = x^2$ translated 1 unit right and 2 units down?

- A $y = -(x - 1)^2 - 2$
- B $y = (x - 1)^2 - 2$
- C $y = -(x + 1)^2 + 2$
- D $y = (x + 1)^2 - 2$

$y = (x - h)^2 + k$
 1 right
 $y = (x - 1)^2$
 2 down
 $y = (x - 1)^2 - 2$

44. Which is the solution set of the equation $x + 2 = \frac{4}{x - 2}$?

- A $\{\pm 2\sqrt{2}\}$
- B $\{2\sqrt{2}\}$
- C $\left\{\frac{-1 \pm \sqrt{17}}{2}\right\}$
- D $\left\{\frac{-1 + \sqrt{17}}{2}\right\}$

$(x + 2)(x - 2) = 4$
 $x^2 - 2x + 2x - 4 = 4$
 $x^2 - 8 = 0$
 $x^2 = 8$
 $x = \pm 2\sqrt{2}$

45. When interest is compounded n times a year, the accumulated amount (A) after t years is given by the formula

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

where P is the initial principal and r is the annual rate of interest.

Approximately how long will it take \$2,000 to double at an annual interest rate of 5.25% compounded monthly?

- A 13.98 years
- B 13.71 years
- C 13.23 years
- D 13.08 years

Handwritten work for Question 45:

$$4000 = 2000\left(1 + \frac{0.0525}{12}\right)^{12t}$$

$$2 = 1.004375^{12t}$$

$$\log 2 = 12t \log 1.004375$$

$$12t = \frac{\log 2}{\log 1.004375}$$

$$12t = 158.7799627$$

$$t = 13.23$$

46. Alan has just started a job that pays a salary of \$21,500. At the end of each year of work, he will get a 5% salary increase. What will his salary be after getting his fifth increase?

- A \$22,631
- B \$24,889
- C \$26,133
- D \$27,440

Handwritten work for Question 46:

$$a_n = a_1 \cdot r^{n-1}$$

$$a_6 = 21,500 \cdot 1.05^{6-1}$$

$$a_6 = 27,440$$

$$a_1 = 21,500$$

$$a_6 = ?$$

$$n = 6$$

$$r = 1.05$$

47. In the function $f(x) = a(x - 4)^2$, where $a > 0$, what happens to the graph of f as the value of a increases?

- A The graph narrows.
- B The graph widens.
- C The graph shifts up.
- D The graph shifts right.

Handwritten note for Question 47: "graph it to see changes!"

48. Which is the inverse of the function $f(x) = x - 9$?

- A $f^{-1}(x) = \frac{1}{x+9}$
- B $f^{-1}(x) = x+9$
- C $f^{-1}(x) = 9-x$
- D $f^{-1}(x) = \frac{1}{x-9}$

Handwritten work for Question 48:

$$y = x - 9$$

$$x = y - 9$$

$$x + 9 = y$$

$$f^{-1}(x) = x + 9$$