

# Adding and Subtracting Rationals Notes

Find the LCM

1)  $x^2y^3$

2)  $a^2b^3c^4$

3)  $(x+1)(x+3)$

4)  $(g-1)(g+4)$

5)  $2r(r+1)$

6)  $w(2w+1)(2w-1)$

7)  $(x+4)(x-2)$

8)  $(x+2)(x+4)(x-3)$

9)  $2(d-3)(d+3)^2$

Adding and Subtracting Fractions

Notes

(1)

1/2 + 1/3 = 5/6

1/2 - 1/3 = 1/6

1/2 + 1/4 = 3/4

1/2 - 1/4 = 1/4

1/3 + 1/6 = 1/2

1/3 - 1/6 = 1/6

1/4 + 1/8 = 3/8

1/4 - 1/8 = 1/8

1/8 + 1/8 = 1/4



$$1. \frac{5 \cdot 4}{6ab \cdot 4} - \frac{7 \cdot 3b}{8a \cdot 3b}$$

$$\frac{20}{24ab} - \frac{21b}{24ab} = \frac{20-21b}{24ab}$$

$$2. \frac{5}{12x^4y} \cdot \frac{1}{5x^2y^3} \cdot 12x^2$$

$$\frac{25y^2}{60x^4y^3} - \frac{12x^2}{60x^4y^3} = \frac{-25y^2 - 12x^2}{60x^4y^3}$$

$$3. \frac{1}{6c^2d} \cdot \frac{3}{4cd^3} \cdot 3c$$

$$\frac{2d^2}{6 \cdot 2c^2d^3} + \frac{9c}{12c^2d^3} = \frac{2d^2 + 9c}{12c^2d^3}$$

$$4. \frac{4m}{3mn} + 2$$

$$\frac{4m}{3mn} + \frac{6mn}{3mn} = \frac{4m + 6mn}{3mn} = \frac{2m(2 + 3n)}{3mn} = \frac{2(2 + 3n)}{3n}$$

$$5. \frac{2x-5}{x+4} - \frac{x-8}{x+4}$$

$$\frac{2x^2 + 3x - 20}{x+4} - \frac{x-8}{x+4} = \frac{2x^2 + 2x - 12}{x+4} = \frac{2(x+3)(x-2)}{x+4}$$

$$6. \frac{4}{a-3} + \frac{9}{a-5}$$

$$\frac{4(a-5) + 9(a-3)}{(a-3)(a-5)} = \frac{4a-20 + 9a-27}{a^2 - 8a + 15} = \frac{13a-47}{(a-3)(a-5)}$$

$$7. \frac{16}{x^2-16} + \frac{2}{x+4}$$

$$\frac{16}{x^2-16} + \frac{2(x-4)}{x^2-16} = \frac{16+2x-8}{x^2-16} = \frac{8+2x}{x^2-16} = \frac{2(x+4)}{(x+4)(x-4)} = \frac{2}{x-4}$$

$$8. \frac{2-5m}{m-9} + \frac{4m-5}{9-m}$$

$$\frac{-2+5m}{9-m} + \frac{4m-5}{9-m} = \frac{-2+5m+4m-5}{9-m} = \frac{9m-7}{9-m}$$

$$9. \frac{y-5}{y^2-3y-10} + \frac{y}{y^2+2y-2}$$

$$\frac{(y-5)(y-1)}{(y-5)(y-1)(y+2)} + \frac{y(y-5)}{(y+2)(y-1)(y-5)}$$

$$\frac{y^2 - 6y + 5}{(y+2)(y-1)} + \frac{y^2 - 5y}{(y+2)(y-1)(y-5)} = \frac{2y^2 - 11y + 5}{(y+2)(y-1)(y-5)}$$



$$10 \quad \frac{5}{2x-12} - \frac{20}{x^2-4x-12}$$

$$\frac{5}{2(x-6)} - \frac{20}{(x-6)(x+2)}$$

$$\frac{5(x+2)}{2(x-6)(x+2)} - \frac{40}{2(x-6)(x+2)} = \frac{5x+10-40}{2(x-6)(x+2)} = \frac{5x-30}{2(x-6)(x+2)}$$

$$= \frac{5(x-6)}{2(x-6)(x+2)} = \frac{5}{2(x+2)}$$

$$11 \quad \frac{2p-3}{p^2-5p+6} - \frac{5}{p^2-9}$$

$$\frac{2p-3}{(p-3)(p-2)} - \frac{5}{(p+3)(p-3)}$$

$$\frac{(2p-3)(p+3)}{(p-3)(p-2)(p+3)} - \frac{5(p-2)}{(p+3)(p-2)(p-3)} = \frac{2p^2+3p-9-(5p-10)}{(p+3)(p-2)(p-3)}$$

$$= \frac{2p^2-2p+1}{(p+3)(p-2)(p-3)}$$

$$12 \quad \frac{1}{5n} - \frac{3}{4} + \frac{7}{10n}$$

$$\frac{4}{20n} - \frac{15n}{20n} + \frac{14}{20n}$$

$$\frac{4-15n+14}{20n} = \frac{-15n+18}{20n}$$

$$= \frac{3(-5n+6)}{20n}$$

$$13 \quad \frac{2a}{a-3} - \frac{2a}{a+3} + \frac{36}{a^2-9}$$

$$\frac{2a(a+3)}{(a-3)(a+3)} - \frac{2a(a-3)}{(a+3)(a-3)} + \frac{36}{(a+3)(a-3)} = \frac{2a^2+12a - (2a^2-6a) + 36}{(a+3)(a-3)}$$

$$\frac{2a^2+12a - 2a^2+6a + 36}{(a+3)(a-3)} = \frac{18a+36}{(a+3)(a-3)} = \frac{12(a+3)}{(a+3)(a-3)} = \frac{12}{a-3}$$

$$\frac{2}{p-q} - \frac{2}{q+p} = \frac{2(p+q) - 2(p-q)}{(p-q)(p+q)} = \frac{2(p+q) - 2p + 2q}{(p-q)(p+q)} = \frac{2q+2q}{(p-q)(p+q)} = \frac{4q}{(p-q)(p+q)}$$

$$\frac{(p+q) - p}{(p-q)(p+q)} = \frac{(p+q) - p}{(p-q)(p+q)} = \frac{q}{(p-q)(p+q)}$$

$$\frac{1+q-p}{(p-q)(p+q)}$$

$$\frac{1}{p+q} + \frac{1}{p-q} = \frac{1}{p+q} + \frac{1}{p-q} = \frac{p-q + p+q}{(p+q)(p-q)} = \frac{2p}{(p+q)(p-q)}$$